INTRODUCTION TO THREE DIMENSIONAL GREOMETRY

- In three dimensions, the coordinate axes of a nectangular Cantesian coordinate system are three mutually penpendicular lines. The axes are called the x, y and z axes.
- The three planes determined by the pair of axes are the coordinate planes, called XY, YZ and ZXplanes.
- The three coondinate planes divide the space into eight pants known as octants.
- The coordinates of a point P in three dimensional Geometry is always written in the form of tniplet like (x, y, z). Hene x, y and z are the distances from the XY, YZ and ZX-planes.
 - (i) Any point on x-axis is of the form (x, 0, 0)
 - (ii) Any point on y-axis is of the form (0, y, 0)
 - (iii) Any point on z-axis is of the form (0,0,z) The coondinates of the onigin 0 ane (0,0,0)
- Signs of the coondinates in eight octant:

| Octants -> Coondinates + | | П | 111 | IV | T | VI | VII | VIII |
|--------------------------|---|---|-----|----|---|----|-----|------|
| χ | + | - | 1 | + | + | 1 | - | + |
| y | + | + | 1 | 1 | + | + | - | 1 |
| Z | + | + | + | + | _ | - | - | = |

Distance between two points P(x,, y,, z,) and Q(x2, y2, z2)

$$\rho \rho = \sqrt{(\chi_2 - \chi_1)^2 + (y_2 - y_1)^2 + (\chi_2 - \chi_1)^2}$$

The coondinates of the point R which divides the line segment joining two points P(x1, y1, x1) and Q (x, y, z) internally and externally in the natio m:n is given by

$$\frac{\left[mx_{2} + nx_{1}, \frac{my_{1} + ny_{1}}{m+n}, \frac{mz_{1} + nz_{1}}{m+n} \right] \text{ and } \left[\frac{mx_{2} - nx_{1}}{m-n}, \frac{my_{2} - ny_{1}}{m-n}, \frac{mz_{2} - nz_{1}}{m-n} \right]$$

- Case I: The coondinates of the mid-point of the line segment joining two points P(x, y, z,) and $Q(x_1, y_1, z_1)$ and $\left[\frac{x_1 + x_2}{x_1 + x_2}, \frac{y_1 + y_2}{x_1 + z_2}\right]$
- Case II: The coondinates of the point R which divides PQ in the natio K:1 ane obtained by taking k = m which are as given below $\frac{kx_2 + x_1}{k}$, $\frac{ky_2 + y_1}{k}$, $\frac{kz_2 + z_1}{k}$
- The coordinates of the centroid of the triangle, whose vertices are $(x_1, y_1, z_1), (x_2, y_2, z_2)$